

Durham Research Online

Deposited in DRO:

15 April 2020

Version of attached file:

Published Version

Peer-review status of attached file:

Peer-reviewed

Citation for published item:

McNulty, R. and Khoze, V. A. and Martin, A. D. and Ryskin, M. G. (2020) 'Isolating the Odderon in central production in high energy pA and AA collisions.', *European physical journal C.*, 80 (3). p. 288.

Further information on publisher's website:

<https://doi.org/10.1140/epjc/s10052-020-7846-5>

Publisher's copyright statement:

This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit <http://creativecommons.org/licenses/by/4.0/>.

Additional information:

Use policy

The full-text may be used and/or reproduced, and given to third parties in any format or medium, without prior permission or charge, for personal research or study, educational, or not-for-profit purposes provided that:

- a full bibliographic reference is made to the original source
- a [link](#) is made to the metadata record in DRO
- the full-text is not changed in any way

The full-text must not be sold in any format or medium without the formal permission of the copyright holders.

Please consult the [full DRO policy](#) for further details.



Isolating the Odderon in central production in high energy pA and AA collisions

R. McNulty¹, V. A. Khoze^{2,3}, A. D. Martin^{2,a}, M. G. Ryskin^{2,3}

¹ School of Physics, University College Dublin, Dublin 4, Ireland

² Institute for Particle Physics Phenomenology, University of Durham, Durham DH1 3LE, UK

³ Petersburg Nuclear Physics Institute, Kurchatov National Research Centre, Gatchina, St. Petersburg 188300, Russia

Received: 17 February 2020 / Accepted: 12 March 2020

© The Author(s) 2020

Abstract We study the rapidity dependence of the central exclusive production cross sections of C-even mesons in pA and AA collisions, where A is a heavy ion. We observe qualitatively different behaviour of the contributions arising from γ -Odderon and Pomeron–Pomeron fusion mechanisms. This can be used to extract the Odderon signal from the events of f_2 mesons exclusively produced in the forward region. Estimates, obtained using expected values of the Odderon cross section, indicate that the γ -Odderon contribution may exceed by a few times the Pomeron-induced background in Pb–Pb collisions. Moreover, the Odderon effect can be clearly seen in terms of the asymmetry in pA and AA collisions with the beam and target reversed. It is particularly interesting to note that the asymmetry for γ -Odderon fusion reaches its maximum value close to 1 in the forward direction, whereas the asymmetry for the Pomeron–Pomeron fusion contribution is small. The role of additional interactions of the f_2 meson with nucleons in the heavy ion, and also the contributions from secondary Reggeons, are estimated. The photon–Odderon contribution has a large normalisation uncertainty but the enhanced cross-section in the forward region combined with a large asymmetry increases the chance of experimentally detecting the Odderon.

1 Introduction

Central exclusive production (CEP) of C-even mesons was intensively discussed as a promising possibility for searching for glueballs produced in Pomeron–Pomeron fusion (see, for example, the reviews in [1–4]). Here we wish to discuss how

this type of process can be used to search for the Odderon.¹ In particular we study the possibility of searching for Odderon-exchange in ultraperipheral pA collisions at the LHC, where A is a heavy ion [19]. It was shown in [19] that the signal cross sections for the semi-exclusive production of C-even mesons due to Odderon- γ fusion could be quite large, up to the μb level – note that the heavy ion enhances the γ flux by a factor Z^2 . So, in principle, the observation of these could be viable search channels for Odderon exchange. However it was also noted in [19] that as well as identifying a sizeable signal, it is essential to quantitatively estimate the contribution from all potential background processes. In addition to production from Odderon- γ fusion we have irreducible backgrounds due to $\gamma\gamma$ and Pomeron–Pomeron fusion, and also a reducible background coming from the photoproduction of vector mesons followed by their radiative decay to the C-even meson where the emitted photon is undetected. If instead of pA collisions, we were to study AA collisions then the background from $\gamma\gamma$ fusion could be overwhelming, whereas in pp collisions the background coming from Pomeron–Pomeron fusion would be strongly dominant. In Ref. [19] the signal and background were estimated for a set of C-even mesons (π^0 , $f_2(1270)$, η , η_c) produced exactly at the centre at rapidity $y = 0$. In each case the background posed a serious challenge to the experiment. Of these, the f_2 meson looked to be the most promising. The cross section is rather large and the backgrounds due to $\gamma\gamma$ -fusion and vec-

¹ The Odderon is the odd-signature ($C = -1$) partner of the even-signature ($C = 1$) Pomeron, see for reviews [5–7]. It is a firm prediction of QCD [8,9], but so far the experimental evidence for its existence is not definitive. There have been various proposals on how to search for Odderon-exchange effects in high energy collisions. In particular, there is a long history of studying the possibility of searching for the Odderon via the exclusive photoproduction of C-even mesons (such as the f_2); see for example [10–18], although no quantitative estimate of the background to the Odderon signal has been made.

^a e-mail: a.d.martin@durham.ac.uk (corresponding author)

tor meson radiative decays (such as $J/\psi \rightarrow f_2 \gamma$) are low.² However the background due to Pomeron–Pomeron fusion still poses a problem.

In this paper, we examine these backgrounds further, as well as those arising from two other sources. In addition we consider the forward kinematics with $y = 2 - 5$ which has some advantages in selecting the Odderon contribution, although here there are increased contributions from the exchange of secondary Reggeons. Since in the forward (i.e. large rapidity y) direction, the rapidity difference between the f_2 meson and the nearest proton is not too large, the $R = \omega$, ρ trajectory exchange is not suppressed too much.

We also consider the viability of looking for an Odderon signal in heavy ion, AA , collisions. The $\gamma\gamma$ fusion background can be controlled by requiring relatively large transverse momenta, $p_t > 0.3 - 0.5$ GeV, of the observed f_2 meson while the Pomeron–Pomeron fusion background in AA case becomes less important. We find that the relative size of the Odderon signal compared to the background is greater in AA than in pA collisions.

We extend our studies in the search for the Odderon making use of the rapidity dependence of photoproduction reactions, to define asymmetries for exclusive f_2 production in both pA and AA central processes. The ability of the LHC to provide beams of protons and ions in either direction, means that forward detectors like LHCb have an acceptance for pA collisions at both positive and negative rapidities. We find a large asymmetry for f_2 production through photon–Odderon fusion that is largely absent in the background Pomeron-induced processes.

We have to emphasize that in the $f_2 \rightarrow \pi^+\pi^-$ decay mode there is a large background coming from the direct $\pi^+\pi^-$ ultraperipheral photoproduction and the higher mass tail of the ρ meson which can be produced via the photon–Pomeron fusion with a quite large cross section. This background has no peak in the f_2 mass region but experimentally it will strongly dilute the significance of the f_2 signal.

The outline of the paper is as follows. In Sects. 2 and 3 we give the formulae for the cross sections for exclusive f_2 production in pA collisions as a function of the f_2 rapidity arising respectively from Pomeron–Pomeron and Photon-induced fusion processes. In Sect. 4 we note that the cross sections have an asymmetry in rapidity; the cross sections $\sigma(pA)$ and $\sigma(Ap)$, with interchanged proton and ion beams, are not equal in the forward direction. In contrast the process $AA \rightarrow A + f_2 + A$ is dominated by $\gamma\gamma$ fusion, and there is no asymmetry in rapidity. However, if we consider events where one of the ions (A^*) is broken then an asymmetry is predicted to occur. Throughout the paper we therefore also

present formulae for the process $AA \rightarrow A + f_2 + A^*$. Note that by A^* we allow for the break up of the ion but not of the constituent nucleons inside the ion. In Sect. 5 we consider the $\gamma\gamma$ background and emphasize that an important background to f_2 production in the $\pi^+\pi^-$ channel is from ρ photoproduction. In Sect. 6 we perform numerical calculations to give indications of the size of the cross sections and asymmetries expected for $pA \rightarrow p + f_2 + A$ and $AA \rightarrow A + f_2 + A^*$ by making physically reasonable assumptions for the unknown parameters. We consider both the Pomeron–Pomeron and the photon-induced fusion mechanisms. The size of the Odderon induced cross section is unknown. However, by using pA and AA collisions and considering the asymmetry of the cross-section with respect to rapidity, its effects can be enhanced.

2 Rapidity dependence of Pomeron–Pomeron fusion

Let us start with the pure exclusive $pp \rightarrow p + f_2 + p$ reaction. The cross section as a function of the rapidity of the f_2 meson has the form

$$\frac{d\sigma_{pp}^{\text{CEP}}}{dy} = \frac{1}{16^2\pi^5} \int d^2p_1 d^2p_2 |A(p_1, p_2, y)|^2 e^{-2(y_1-y_2)} \quad (1)$$

where y_1 (y_2) and y are the rapidities of the beam (target) protons and f_2 meson respectively ($y_1 > y > y_2$); and p_1 (p_2) are the transverse momenta of the outgoing protons; $t_1 = -p_1^2$, $t_2 = -p_2^2$. The amplitude is dominated by double Pomeron exchange and reads

$$A(p_1, p_2, y) = C \exp(Bt_1 + Bt_2) e^{\alpha_P(t_1)(y_1-y)} e^{\alpha_P(t_2)(y-y_2)}, \quad (2)$$

where $\alpha_P(t)$ is the Pomeron trajectory; B accounts for the slope of the vertices and C is the product of the coupling constants (two Pomeron–proton couplings times the Pomeron–Pomeron-to- f_2 fusion constant). For the Pomeron trajectory we use the simple form $\alpha_P(t) = 1 + \epsilon + \alpha'_P t$ with $\alpha'_P = 0.25$ GeV⁻² and $\epsilon = 0.0808$ (corresponding to the Donnachie–Landshoff (DL) parametrization [20,21]). After integration over the transverse momenta in (1) the cross section becomes

$$\frac{d\sigma_{pp}^{\text{CEP}}(y)}{dy} = \frac{C^2}{16^2\pi^3} \frac{e^{2\epsilon(y_1-y_2)}}{4(B + \alpha'_P(y_1-y))(B + \alpha'_P(y-y_2))}. \quad (3)$$

The only rapidity dependence comes from the denominator of (3). Taking $B = 8$ GeV⁻² (which is consistent with the WA102 data [22]) we expect a rather weak y -dependence.

² Note that in Table 3 of [19] the background caused by $\gamma\gamma$ fusion was underestimated by a factor of 5, but this contribution is still much lower than the Pomeron–Pomeron term.

At $\sqrt{s} = 13$ TeV the cross section increases by 1.3% going from $y = 2$ to $y = 5$. This is negligible.

2.1 pA collisions

A stronger y dependence is expected in heavy ion collisions when we account for the possibility of interaction of the f_2 meson with the ion (or rather with the nucleons, N , in the ion). First we consider the exclusive process $pA \rightarrow p + f_2 + A$. The probability of the above ‘secondary’ interaction is driven by the $\sigma(f_2N)$ cross section, which increases with energy, that is with the f_2 rapidity as $\exp(2\epsilon(y - y_2))$ (here the rapidity of target ion $y_2 < 0$ is negative).

Besides this we have to account for the additional beam-target inelastic interactions which populate the rapidity gap and thus violate the ‘exclusivity’ condition. The corresponding ‘gap survival probability’, S^2 , for the case of collisions with a heavy ion was discussed in detail in [23]. It is convenient to calculate the value of S^2 in impact parameter, b_t , space. For the case of survival against an additional proton-ion interaction³

$$S_{pN}^2(b_t) = \exp(-\sigma_{\text{tot}}(pN) T_A(b_t)), \quad (4)$$

where $\sigma_{\text{tot}}(pN)$ is the total cross section of the proton–nucleon interaction and $T_A(b)$ is the optical density of the heavy ion,

$$T_A(b) = \int_{-\infty}^{\infty} dz (\rho_p(z, b) + \rho_n(z, b)). \quad (5)$$

In this simplified estimate we neglect the radius, r_{pN} , of the proton–nucleon interaction in comparison with the larger heavy ion (A) radius and consider the *total* exclusive cross section integrated over t_1 and t_2 .

The nucleon density distribution in A is described by the Woods-Saxon form [26]

$$\rho_N(r) = \frac{\rho_0}{1 + \exp((r - R)/d)}, \quad (6)$$

where the parameters d and R respectively characterise the skin thickness and the radius of the nucleon density in the heavy ion; $r = (z, b)$. For ^{208}Pb we take the recent results of [27, 28]

$$\begin{aligned} R_p &= 6.680 \text{ fm}, & d_p &= 0.447 \text{ fm}, \\ R_n &= (6.67 \pm 0.03) \text{ fm}, & d_n &= (0.55 \pm 0.01) \text{ fm}. \end{aligned} \quad (7)$$

³ We do not include the inelastic Glauber corrections since the effect of inelastic shadowing is almost compensated by the effect of short-range correlations in the wave function of the target nucleus [24, 25].

The nucleon densities, ρ , are normalized to

$$\int \rho_p(r) d^3r = Z, \quad \int \rho_n(r) d^3r = N_n, \quad (8)$$

for which the corresponding proton (neutron) densities are $\rho_0 = 0.063$ (0.093) fm^{-3} .

Correspondingly the probability to preserve the exclusivity against f_2N additional interactions with the target ion is given by

$$S_{f_2N}^2(b) = \exp(-\sigma_{\text{tot}}(f_2N) T_A(b)), \quad (9)$$

where $\sigma_{\text{tot}}(f_2N)$ is the cross section of an f_2 meson interacting with a nucleon, N , in the ion.

To calculate the rapidity dependence of f_2 production in proton- A collisions we first compute the cross section for the incoherent process, $pA \rightarrow p + f_2 + A^*$, where the outgoing ion, A^* , breaks up. This cross section is given by that for the CEP in pN collisions, $d\sigma_{pp}^{\text{CEP}}/dy$, times the number of nucleons in the ion at fixed b_t (i.e., $T_A(b)$) times the survival factors describing no additional pA and f_2A interactions (i.e., the survival against the production of additional secondaries). Thus integrating over b_t we have

$$\frac{d\sigma_{pA}^{\text{incoh}}}{dy} = \frac{d\sigma_{pp}^{\text{CEP}}}{dy} \int d^2b T_A(b) S_{f_2N}^2(b) S_{pN}^2(b), \quad (10)$$

where S_{pN}^2 is given by (4) and $S_{f_2N}^2$ is given by (9). Strictly speaking we should account for the gap survival factor, S_{pp}^2 , in the proton-proton case as well. However in this case it can be included in the constant C , that is into the $d\sigma_{pp}^{\text{CEP}}/dt$ value, which anyway should be taken from experiment.

The cross section for the coherent (‘elastic’) process, $pA \rightarrow p + f_2 + A$ is a little more difficult to calculate. We have first to calculate the amplitude, which is proportional to the total number of nucleons ($\int d^2b T_A(b)$) in the incoming ion. After integration over the momentum q_t transverse to the incoming ion we obtain the factor $\delta(b - b^*)$, where b and b^* are the independent impact parameters of the contributing nucleons in the amplitude A and the complex conjugate amplitude A^* , respectively. Finally we obtain

$$\frac{d\sigma_{pA}^{\text{coh}}}{dy} = \frac{d\sigma_{pp}^{\text{CEP}}}{dy} 8\pi(B + \alpha'_p(y - y_2)) \int d^2b T_A^2(b) S_{f_2N}^2(b) S_{pN}^2(b), \quad (11)$$

where the optical density T_A is now squared and the extra dimension due to the extra T_A is compensated by the slope of the NN cross section, $2(B + \alpha'_p(y - y_2))$. The details of the calculation can be found in [23].

Note that the rapidity dependence is hidden in the energy/rapidity behaviour of the slope $2\pi(B + \alpha'_p(y - y_2))$ and in the cross section $\sigma_{\text{tot}}(f_2N)$ that enters the survival factor (9).

2.2 AA' collisions

For f_2 production in ion-ion collisions, $AA' \rightarrow A + f_2 + A'$, we have a third survival factor

$$S_{f_2 N'}^2(b_2) = \exp(-\sigma_{\text{tot}}(f_2 N') T_{A'}'(b_2)), \quad (12)$$

where N' denotes a nucleon in the target ion, while $T_{A'}'(b_1)$ is the target ion optical density. As before, working in the b_t representation, the central incoherent (with respect to both A and A' ions) cross section for $AA' \rightarrow A^* + f_2 + A'^*$ reads

$$\frac{d\sigma_{AA'}^{\text{incoh}}}{dy} = \frac{d\sigma_{pp}^{\text{CEP}}}{dy} \times \int d^2b_1 d^2b_2 T_A(b_1) T_{A'}'(b_2) S_{f_2 N}^2(b_1) S_{f_2 N'}^2(b_2) S_{NN'}^2(|\vec{b}_1 - \vec{b}_2|), \quad (13)$$

where the factor $S_{NN'}^2$ accounts for the rescattering of constituent nucleons in the incoming beam and target ions. (Recall that the incoherent cross section is normalised to pure central exclusive pp collisions, which do not include proton excitations. Therefore in the above process A^* means that the ion is broken but that the constituent nucleons in the ion remain intact.) For ion-ion collisions the survival factor

$$S_{NN'}^2(b) = \exp(-\sigma_{\text{tot}}(NN) \Omega_{AA'}(b)), \quad (14)$$

with

$$\Omega_{AA'}(b) = \int d^2b_1 d^2b_2 T_A(b_1) T_{A'}'(b_2) \delta^{(2)}(\vec{b} - \vec{b}_1 + \vec{b}_2). \quad (15)$$

As shown in [23] (see Fig. 4(right)) for the lead-lead interactions $S_{NN'}^2(b) \simeq \theta(b - 17 \text{ fm})$; that is, it is close to the form of a θ function.

Correspondingly the coherent (with respect to A) $AA' \rightarrow A + f_2 + A'^*$ cross section is obtained by a similar replacement in (11) leading to the form

$$\frac{d\sigma_{AA'}^{\text{coh}}}{dy} = \frac{d\sigma_{pp}^{\text{CEP}}}{dy} 8\pi(B + \alpha'_p(y_1 - y)) \int d^2b_1 d^2b_2 T_A^2(b_1) T_{A'}'(b_2) S_{f_2 N}^2(b_1) S_{f_2 N'}^2(b_2) S_{NN'}^2(|\vec{b}_1 - \vec{b}_2|). \quad (16)$$

Recall that rapidity dependence is hidden in the energy/rapidity behaviour of the $\sigma_{\text{tot}}(f_2 N)$ cross section that enters the survival factors (9, 12).

We note that the values of the integral in (10) and (13) can be treated as effective numbers of nucleon-nucleon pairs (nucleons from the heavy ion) that produce the f_2 meson. The same is true for the factor $8\pi(B + \alpha'_p(y_1 - y))$ times the integral (i.e. the whole r.h.s expression, except for the factor

$d\sigma_{pp}^{\text{CEP}}/dy$) in Eqs. (11) and (16)). See [23] and sect. 6.1 of [19] for more discussion of the formulae in this section.

2.3 Missing information in the survival factors

Unfortunately the cross section $\sigma_{\text{tot}}(f_2 N)$ is not known. One possibility is to assume that it is equal to the pion-proton cross section described by the Donnachie-Landshoff parametrization [20,21]

$$\sigma_{\text{tot}}(f_2 N) = \sigma_0 (s/1 \text{ GeV}^2)^\epsilon \quad (17)$$

with $\sigma_0 = 13.6 \text{ mb}$ and $\epsilon = 0.0808$. Another possibility is to say that $\sigma_{\text{tot}}(f_2 N) = \sigma_{\text{tot}}(\rho N)$ where the ρ -proton cross section is extracted from the ρ meson diffractive photoproduction data [29] in the framework of the Vector Dominance Model (VDM) [30,31]. This gives $\epsilon = 0.055$ and $\sigma_0 = 15.7 \text{ mb}$, which defines the VDM form of $\sigma_{\text{tot}}(f_2 N)$. However even this value (which is a bit smaller in the relevant energy region) can be an overestimate. It is not excluded that the wave function of the f_2 meson produced via Pomeron-Pomeron fusion has not at the outset its normal configuration, but rather is represented by the small size, \hat{r} , of the quark-antiquark pair which has a lower cross section ($\sigma \propto \alpha_s^2 \langle \hat{r}^2 \rangle$, see [32,33]) than that of the finally formed meson in its 'equilibrium' state. Therefore in our numerical estimates we will use also the absorptive cross section with $\sigma_0 = 15.7/2 \text{ mb}$, half the value of that given for the ρ meson by VDM.

2.4 Including secondary Reggeon contributions

Besides f_2 production by Pomeron-Pomeron fusion there are production amplitudes in which one or both Pomerons in the amplitude (2) can be replaced by a secondary Reggeon⁴ of the form

$$A_R(p_1, p_2, y) = C_R \exp(B't_1 + B''t_2) e^{\alpha_R(t_1)(y_1 - y)} e^{\alpha_P(t_2)(y - y_2)}. \quad (18)$$

After the integration over the transverse momenta (analogous to going from (2) to (3)) we find that the rapidity dependence is now is suppressed by the factor $\exp((\alpha_{f_2} - 1)(y_1 - y))$ or $\exp((\alpha_{f_2} - 1)(y - y_2))$, due to a smaller intercept $\alpha_R(0) = \alpha_{f_2}(0) \simeq 0.5$. Hence it is negligible for a large rapidity interval $y_1 - y$. However in the forward direction, for example at a rapidity of 5 where the rapidity difference $y_1 - y$ is 3.5–4.5, the interference of secondary Reggeon with Pomeron exchange may affect the rapidity distribution of the produced

⁴ Sometimes the secondary Reggeon, $R = f_2$, is said to lie on the so-called P' trajectory.

f_2 meson enlarging the cross section at larger $|y|$. The effect may be more important if for some reason the ‘Pomeron–Pomeron $\rightarrow f_2$ ’ vertex is much smaller than the ‘Pomeron– $R \rightarrow f_2$ ’ vertex. Such a situation may occur if it happens that the f_2 CEP follows a pattern of a purely perturbative expectation, derived for the case of the 2^{++} state formed by the heavy quarks, see e.g. [34,35].

The contribution of secondary Reggeons should be clearly seen in the rapidity y -distribution as a fast growth of the cross section as y increases towards the higher end of rapidity interval.

Note that within the perturbative approach a heavy 2^{++} quarkonium is produced by fusing gluons from the colliding Pomerons; for a review see e.g. [36]. An important property of the perturbative CEP mechanism [37] is that in the forward proton limit the centrally produced state should obey the so-called $J_z^{PC}=0^{++}$ selection rule (J_z is the projection of its spin onto the collision axis). If the zero helicity diphoton (digluon) transition to the 2^{++} quark–antiquark state is suppressed (which is true only in the non-relativistic quark approximation) then we could expect the suppression of the tensor state CEP in the proton–proton collisions. Though a priori being far from obvious, it was shown (see e.g. [38,39]) that even in the case of light quarks, the helicity zero amplitude for the $\gamma\gamma$ coupling of the $q\bar{q}$ tensor mesons remains numerically small, and this was experimentally confirmed by the BELLE collaboration [40] in the high-statistics measurement of the dipion production in photon–photon collisions.

It is quite intriguing that while the $f_2(1270)$ CEP was clearly seen in the ISR measurement at $\sqrt{s} = 62$ GeV using the Split Field Magnet spectrometer [41,42], the f_2 signal disappears in the study with the Axial Field spectrometer at the same energy but when the protons were scattered nearly forward [43,44]; that is here we are close to $J_z = 0$ kinematics. A vanishing of the f_2 signal at low momentum transfer to scattered protons was observed also in the E690 fixed target experiment at the Tevatron at $\sqrt{s} = 40$ GeV (see e.g. [45]).⁵ A further indication along this line follows from the preliminary LHCb measurement [47] of dipion central production in p Pb collisions at 8.16 TeV. While the f_2 signal is clearly seen when no special exclusivity requirement is imposed, it is strongly suppressed when there is no observed activity in the forward region. Such a peculiar behaviour of the $f_2(1270)$ CEP at low momentum transfers certainly needs further detailed investigation in particular at the LHC energies with the dedicated forward proton detectors TOTEM and ALFA. Thus in comparison with the Pomeron–Pomeron CEP amplitude (2) the Pomeron– R term most probably has a constant factor C_R about a factor 1 to 4 larger than C .

⁵ We are grateful to Mike Albrow for bringing our attention to this phenomenon, see also [46].

3 Rapidity dependence of photon-induced f_2 production

C-even mesons can be produced in exclusive events either via the fusion of two C-even objects (Pomeron–Pomeron) or two C-odd objects (γ -Odderon or $\gamma - R$ where $R = \rho$ or ω). The photon flux, N_γ , radiated by the lead ion is quite large - it is enhanced by a $Z^2 = 82^2$ factor and is a strong function of photon energy (rapidity). In b_t space, which is convenient to account for the survival factors S^2 , the photon flux outside the heavy ion⁶ reads [48,49]

$$\frac{d^3 N_\gamma}{dx d^2 b_\gamma} = \frac{Z^2 \alpha^{\text{QED}}}{x \pi^2 b_\gamma^2} (x m_n b_\gamma)^2 K_1^2(x m_n b_\gamma). \quad (19)$$

Here $K_1(z)$ is the modified Bessel function of the first kind; x is the nucleon momentum fraction carried by the photon; b_γ is the b_t position of the f_2 production vertex with respect to the centre of the ion; and m_n is the nucleon mass. For large z the function $K_1(z) \propto e^{-z}$ decreases exponentially. However the values of x relevant for central f_2 production at the LHC are very small

$$x \sim m_{f_2} e^{-y}/\sqrt{s} \sim 10^{-4}. \quad (20)$$

Note that $z = 1$ corresponds to $b_\gamma \gtrsim 200$ fm. Thus the dominant contribution has a logarithmic $d^2 b_\gamma / b_\gamma^2$ structure and comes from very large b_γ starting at $b_\gamma = R_A$ ($2R_A$ for AA collisions) and up to $b_\gamma \sim 1/x m_n$ for the case of proton-ion (ion-ion) collisions; R_A is the ion radius.

3.1 Photon–Odderon fusion

Our particular interest is in f_2 production by γ -Odderon fusion so let us discuss this first. For the large values of b_γ mentioned above we can neglect the survival factors with respect to the ion which emits the photon. Hence we can put the survival factors

$$S_{NN'}^2 = S_{pN}^2 = S_{f_2 N}^2(b_\gamma) = 1 \quad (21)$$

and write the CEP cross section just as the product of the photon flux times the Odderon induced, σ_{Odd} , cross section

$$\frac{d\sigma_{\text{Odd}}}{dy} = \frac{dN}{dy} \sigma_{\text{Odd}}(\gamma D \rightarrow f_2 D), \quad (22)$$

where D denotes the proton in the case of pA collisions or the ion A' in the AA' case.

⁶ For small $b_t < R_A$ the contribution to the exclusive cross section is strongly suppressed by the gap survival factors S^2 .

Recall that the lead ion A radiates the photon *coherently* and is not destroyed (otherwise we lose the large factor $Z = 82$). On the other hand it is better to select the events of *incoherent* interactions with the ion A' . In this way we suppress the background caused by $\gamma\gamma \rightarrow f_2$ fusion. The incoherent events can be selected by observing the signal in the rapidity interval close to the A' ion or by looking for the events with a relatively large transverse momentum of the f_2 meson, say, $p_{t,f_2} > 0.3 - 0.4$ GeV. (Recall that $p_{t,\gamma}$ is still quite small due to the large values of b_γ ; therefore p_{t,f_2} is almost equal to the momentum transferred to A').

Since the Odderon intercept, α_{Odd} , is very close to 1 [5,6,50], the rapidity dependence of the photon–Odderon fusion cross section in pA collisions is completely driven by the behaviour of the photon flux dN/dy . In the AA' case the gap survival factor $S_{f_2N'}^2$ also has an effect. Indeed, the semi-exclusive $\gamma A' \rightarrow f_2 A^*$ cross section reads

$$\sigma(\gamma A' \rightarrow f_2 A^*) = \sigma_{\text{Odd}}(\gamma p \rightarrow f_2 p) \int d^2 b T_{A'}'(b) S_{f_2N'}^2(b), \quad (23)$$

where A^* denotes the ion A' , after it was broken by the incoherent interaction, and $S_{f_2N'}^2$ is given by (12).

3.2 γ - R fusion

Of course the Odderon exchange in (22, 23) can be replaced by C-odd secondary Reggeon $R = \omega$ (or $R = \rho$) exchange. We get exactly the same expressions (Eqs. (22) and (23)). The only difference is that the ‘elementary’ cross section $\sigma_R(\gamma p \rightarrow f_2 p)$ (which replaces σ_{Odd} in Eqs. (22, 23)) now depends on the f_2 -proton energy, that is on the rapidity of the f_2 meson as

$$\sigma_R(\gamma p \rightarrow f_2 p) \propto \exp(2(\alpha_R - 1)(y_1 - y)). \quad (24)$$

This leads to a strong rapidity dependence of the secondary Reggeon-exchange contribution. At LHC energies this contribution is completely negligible at central rapidities (that is, y close to 0 in the laboratory frame) but may reveal itself in the forward region where the difference $|y_1 - y|$ becomes smaller and the exponential increase towards 1.

Besides this there may be interference between different contributions. The interference between the Pomeron and the Odderon is small since the Pomeron-exchange amplitude is mainly imaginary while the Odderon-exchange is real. On the other hand secondary Reggeon-exchange can interfere with both the Pomeron and the Odderon amplitudes. However below we will neglect the interference effects in our simplified numerical estimates.

4 Asymmetry

The differential cross-sections for exclusive f_2 production described above exhibit very different dependencies with rapidity. That resulting from Pomeron–Pomeron fusion is rather flat, while photon–Odderon production has a strong dependence due to the photon flux. For proton-ion collisions this can be usefully encoded in an asymmetry, A , defined as

$$A(pA) = \frac{\sigma(pA) - \sigma(Ap)}{\sigma(pA) + \sigma(Ap)}, \quad (25)$$

where $\sigma(pA)$ and $\sigma(Ap)$ denote the cross sections measured in runs with interchanged proton and ion beams (at the same y_{f_2}).

In pp collisions and AA collisions (where the ions remain intact) the asymmetry is absent ($A=0$). However in ion-ion collisions we can have asymmetry by selecting events where one ion (A^*) is broken while the other one (A) remains intact:

$$A(AA^*) = \frac{\sigma(A^*A) - \sigma(AA^*)}{\sigma(A^*A) + \sigma(AA^*)}. \quad (26)$$

4.1 Pomeron–Pomeron fusion

Due to the small value of α'_p , we may neglect the small rapidity dependence of the t -slopes and hence the proton–nucleon amplitude (2) has no asymmetry. However, an asymmetry appears after we account for the survival factors S^2 in (10). Indeed, the probability to have no additional interactions of the f_2 meson with the nucleons inside the heavy ion decreases when the cross section σ_{f_2N} increases (see (9)); i.e., when the rapidity difference $y - y_2$ (or $y_1 - y$) becomes larger. This means that we expect a larger cross section (10) in the case when the forward f_2 goes in the direction of the ion. Let us denote this case as (pA) so the corresponding asymmetry, A , is *positive*.

For ion-ion collisions the situation is a bit more complicated. We have the survival factors $S_{f_2N}^2$ and $S_{f_2N'}^2$ from both sides (both ions). However in (16) the optical density $T_A(b_1)$ is squared. That is the typical values of $T_A(b_1)$ in the unbroken ion are larger than, $T_{A'}(b_2)$, in the ion that was destroyed. Therefore the factor $S_{f_2N}^2(b_1)$ becomes more important and the f_2 meson would prefer to fly in the direction of the unbroken ion (which interacts coherently).

4.2 Photon–Odderon fusion

For photon induced processes the cross section is proportional to the photon flux N_γ (19), which increases with x decreasing. This effect is stronger than that caused by the S^2 factors. Therefore now the cross section is larger when the f_2 meson goes in the direction opposite to the ion that was not

destroyed and ‘coherently’ radiates the photon. This leads to a *negative* asymmetry A .

4.3 Fusion with a secondary Reggeon

Recall that for proton–ion collisions at the LHC the energy per nucleon for the lead beam is about 2.5 times smaller than the proton beam energy. This leads to an additional asymmetry. Since the R -exchange cross section decreases with energy (that is with the rapidity difference) the R -exchange contribution is larger for kinematics in which the f_2 meson goes in the ion direction; hence adding some *positive* component to the asymmetry $A(pA)$.

5 Backgrounds

When searching for the Odderon contribution in exclusive f_2 production we face two obvious sources of background. These arise from the production of the f_2 meson by Pomeron–Pomeron fusion and $\gamma\gamma$ fusion. In the next Section we will give indicative estimates of the size of the contribution arising from Pomeron–Pomeron fusion using the formalism that we developed in Sect. 2. We first discuss the background from $\gamma\gamma$ and γ -Pomeron fusion.

5.1 $\gamma\gamma$ fusion

It must be mentioned that Odderon exchange can be replaced by the photon exchange. Such a photon–photon fusion contribution can be calculated with rather good accuracy based on the known $f_2 \rightarrow \gamma\gamma$ decay width. This gives

$$\frac{d\sigma_{\text{QED}}(\gamma p \rightarrow f_2 + p^*)}{dt} = \frac{0.23 \text{ nb}}{|t|} F_{\gamma\gamma \rightarrow f_2}^2(t), \quad (27)$$

where p^* indicates that we allow the proton to dissociate into some low mass state p^* (since on this side we are looking for the ‘incoherent’ process). For this reason we omit the proton form factor in (27).

Practically it is impossible to distinguish here between the photon and the Odderon exchanges. Formally in the case of a photon we have an extra $1/t$ factor in (27) and may expect a steeper t -dependence. On the other hand we do not know the $F_{\gamma\gamma \rightarrow f_2}^2(t)$ form factor and already we have selected not too small $|t|$. Note that the trivial $\gamma\gamma$ contribution will have the same y -behaviour as that for Odderon exchange. Integrating over the $0.3 < p_{t,f_2} < 1$ GeV, it must be normalized to $\sigma \simeq 0.3 - 0.4$ nb instead of $\sigma_{\text{Odd}}(\gamma p \rightarrow f_2 p) = 1$ nb which will be used for the numerical estimates in Sect. 6. The value taken for the cross section σ_{Odd} is discussed in Sect. 6.1.

5.2 γ -Pomeron fusion

For photon-induced production, the f_2 peak is placed on the top of a large background coming from the tail of $\rho(770)$ meson ultraperipheral photoproduction (the ρ meson is produced via the photon–Pomeron fusion with a rather large cross section). In particular, taking $\sigma(\gamma p \rightarrow \rho p) \simeq 10 \mu\text{b}$ measured at HERA [51], we expect the ρ -photoproduction induced $\pi^+\pi^-$ cross section, in the interval $M(f_2) \pm \Gamma(f_2)/2$, to be $\sigma \simeq 270$ nb. How does this compare with $f_2 \rightarrow \pi^+\pi^-$ production via Odderon exchange? There are, at present, no data for $\sigma(\gamma p \rightarrow f_2 p)$, but experimental limits of 16 nb [52] indicate that the value is much smaller than from the tail of the ρ resonance. We discuss this further in Sect. 6.1.

Clearly, in order to separate out a pure f_2 signal it would be desirable to perform the partial wave analysis selecting a $J^P = 2^+$ state. However with such a large contribution from other partial waves it would be difficult and require very large statistics. A possible way to avoid the serious ρ background would be to seek events for the f_2 meson via its $\pi^0\pi^0$ and KK decay modes.

6 Numerical estimates

To get an impression for the size of the cross sections and asymmetries we present in Figs. 1, 2, 3 and 4 the results of some numerical calculations. These plots are shown for illustration. Unfortunately, as mentioned, we do not know the size of the Odderon-photoproduced cross section, σ_{Odd} ; nor the values of the required couplings, like

$$PP \rightarrow f_2, \quad PR \rightarrow f_2, \quad \gamma O \rightarrow f_2, \quad \gamma R \rightarrow f_2, \quad (28)$$

where P , O and R denote Pomeron, Odderon and Reggeon, respectively. Also we do not know the cross section $\sigma_{\text{tot}}(f_2 N)$ where N is a nucleon. Therefore we plot the contributions of the different components separately. We consider ‘13 TeV’ kinematics, that is the proton beam has 6.5 TeV energy while the energy of the nucleon in the lead ion is 2.56 TeV.

6.1 Input assumptions and notation for the curves in the figures

The cross section for the photoproduction of the f_2 meson by Odderon-exchange is the largest unknown in our predictions concerning the proposed search for the Odderon in pA and AA collisions. A reasonable rough estimate is

$$\sigma_{\text{Odd}}(\gamma p \rightarrow f_2 p^*) \sim 1 - 10 \text{ nb}. \quad (29)$$

Expectations based on lowest-order QCD give values in the region of 1 nb, whereas HERA data [52] give an upper limit of

16 nb. For our numerical estimates below we will normalize our predictions to 1 nb; these are then easy to scale up or down as appropriate.

To evaluate the cross section of central f_2 production via Pomeron–Pomeron fusion we normalize the first factor, C , in (2) to be in agreement with the CMS data [53]. Thus we take

$$d\sigma(f_2)/dy = 1 \mu\text{b} \quad \text{at } y = 0. \quad (30)$$

In such a form it will be easy to recalculate the result expected in the case of another value of C or $d\sigma(f_2)/dy$. For the R -contribution we put $C_R = 2C$ and $\alpha_R(0) = 1/2$ in (18). Thus the ratio of the fusion amplitudes is given by

$$\frac{\text{PR amplitude}}{\text{PP amplitude}} = 2/\sqrt{s_{f_2 N}/1\text{GeV}^2}. \quad (31)$$

The absorptive cross section $\sigma_{\text{tot}}(f_2 N)$ is chosen in three different ways: via the VDM approach (17) with $\sigma_0 = 15.7$ mb, with a twice smaller $\sigma_0 = 15.7/2$ mb (taking $\epsilon = 0.055$), and with no absorption inside the heavy ion ($\sigma_0 = 0$).

The γ -Odderon induced cross section is normalized to $\sigma(\gamma + p \rightarrow f_2 + p^*) = 1$ nb. We use the VDM to evaluate the Reggeon contribution. It gives

$$\frac{\gamma R \text{ amplitude}}{\gamma O \text{ amplitude}} \simeq 5/\sqrt{s_{f_2 N}/1\text{GeV}^2}, \quad (32)$$

where here the R -Reggeon is ω , ρ .

To search for the Odderon we have to keep one ion unbroken in order to have coherent photon radiation. Therefore we consider AA^* and/or Ap final state configurations. However the A^*A^* contribution (with both ions incoherent) is also shown in Fig. 1 by the dashed curve for comparison.

Note that, to enlarge the statistics, in our estimates we allow also some low mass excitations of the nucleons. That is, when discussing CEP processes we bear in mind CEP* (which includes low mass excitations similar to [19]). In all the figures the rapidity of the f_2 meson is defined to be positive if the f_2 is going in the direction of the proton for pA collisions and in the direction of A^* for the AA^* case.

6.2 Results for the cross section and the asymmetry

The figures are based on the parameters described above. Figs. 1 and 2 show the contributions to the cross section $d\sigma/dy$ for the process $AA \rightarrow A + f_2 + A^*$, while Fig. 3 shows the results for $pA \rightarrow p^* + f_2 + A$. The contributions to the asymmetries in f_2 rapidity for the respective processes are compared in the two plots of Fig. 4.

We start with the discussion of Fig. 1. It shows the exclusive production of the f_2 ($y = -5.5$ to 5.5) in PbPb collisions. Assuming (22) with $\sigma_{\text{Odd}} = 1$ nb, the Odderon-

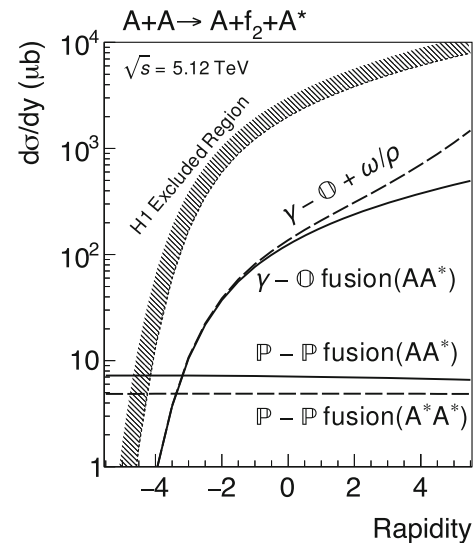


Fig. 1 Indicative predictions for the photon- and Pomeron-induced cross sections for the (incoherent) process $AA \rightarrow A + f_2 + A^*$ as a function of the f_2 rapidity for $\sqrt{s_{NN}} = 5.12$ GeV. In this plot the f_2 absorptive cross section $\sigma_{\text{tot}}(f_2 N)$ in the heavy ion is calculated from (17) with $\sigma_0 = 15.7/2$ mb and $\epsilon = 0.055$. The dashed curve for (A^*A^*) is shown only because this process serves as a possible background to the Pomeron-induced (AA^*) contribution. The shaded band indicates the region predicted to be excluded for the Odderon signal if we were to use the upper limit for $\sigma(\gamma p \rightarrow f_2 p)$ of 16 nb found at HERA [52], rather than 1 nb

induced cross section⁷ in the forward region is an order-of-magnitude larger than that driven by Pomeron–Pomeron fusion. Secondary Reggeons (shown by dot-dashed curve for γ -induced production) may noticeably enlarge (about 2 times at $y = 4$) the cross section in the forward region, where the suppression of the amplitude, $\exp((y_1 - y)/2)$ is not too strong, while the coupling to the secondary Reggeon may be quite large, see (32).

The dependence of the predictions on the f_2 absorption cross section is shown in Fig. 2. Of course larger absorption leads to a smaller cross section of f_2 meson production, as seen from the figure. Note that for the γ -induced component we have stronger absorption. Indeed, for Pomeron–Pomeron fusion the major contribution comes from the region $b_1, b_2 \sim R_A$, see (16). That is the f_2 is created on the periphery of both ions where the optical density $T_A(b)$ is not large. On the contrary for the γ -induced component we deal with large b_γ ; that is, there is practically no absorption by the ion A , but the integral over the parameter b_2 (b in (23)) covers the whole transverse area of the ion A^* . Hence in the survival factor (12) we have a much larger optical density T_{A^*} . Therefore the dependence of the γ -induced curves on σ_0 is greater.

⁷ For comparison we also show by the shaded band the upper limit of the Odderon-exchange signal if we were to use the HERA H1 limit of 16 nb [52] for the f_2 photoproduction cross section via Odderon exchange.

Fig. 2 The shift of the continuous curves show the effect of changing $\sigma_{\text{tot}}(f_2 N)$ from 0 to the VDM form of (17) with $\sigma_0 = 15.7$ mb and $\epsilon = 0.055$. The dashed curves show the possible effect of including a secondary Reggeon contribution. Note that the two plots, showing respectively the Pomeron- and photon-induced contributions to $AA \rightarrow A + f_2 + A^*$, have the same scale

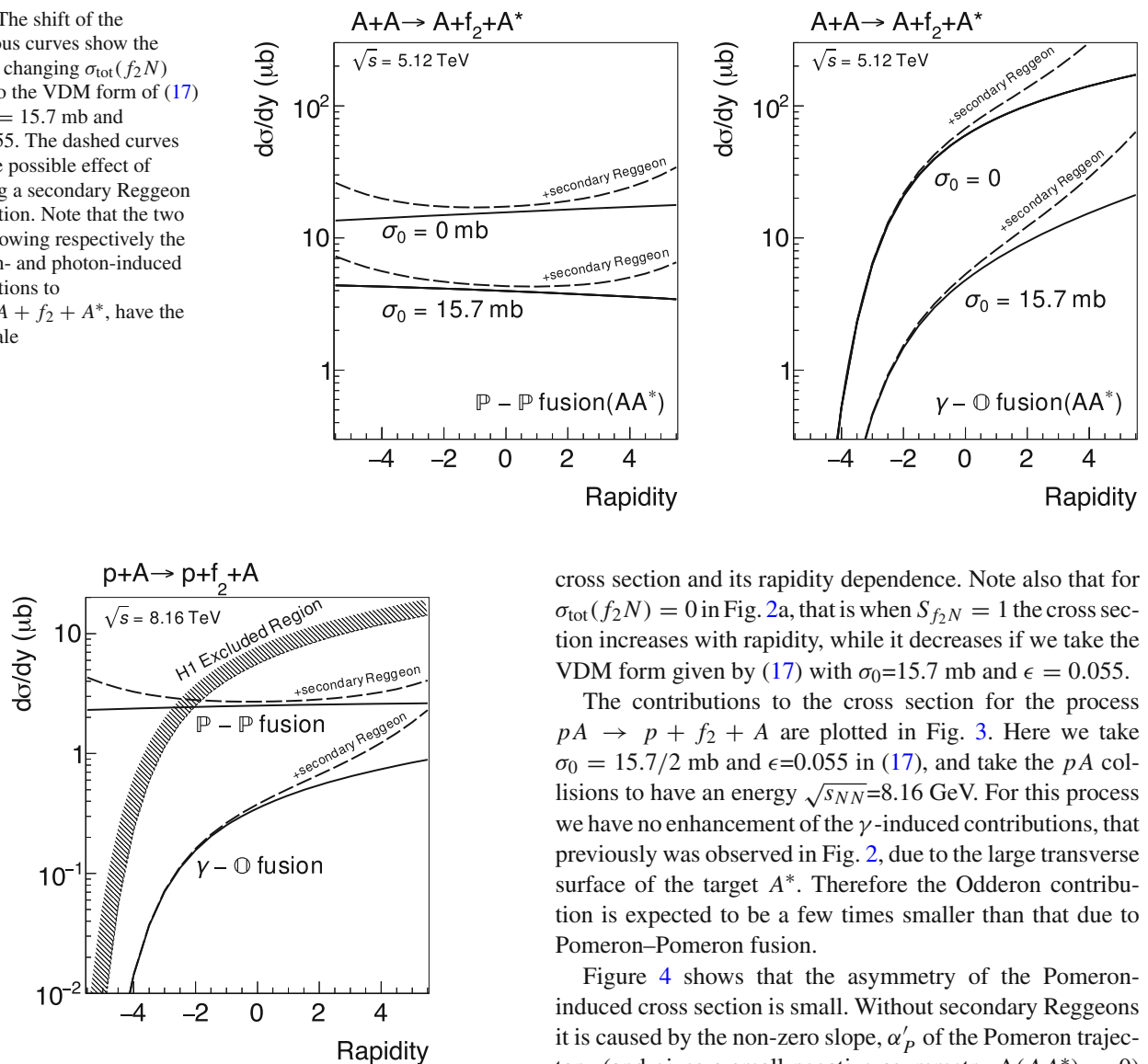


Fig. 3 Indicative predictions of the Pomeron-Pomeron fusion and γ -Odderon fusion contributions to the cross section for $pA \rightarrow p + f_2 + A$ as a function of the f_2 rapidity for $\sqrt{s_{NN}} = 8.16$ GeV. The dashed curves show the effect of including a secondary Reggeon contribution. The effect of changing the absorptive cross section $\sigma_{\text{tot}}(f_2 N)$ has a smaller effect than that for AA' collisions which was shown in Fig. 2. Here we take $\sigma_{\text{tot}}(f_2 N)$ from (17) with $\sigma_0 = 15.7/2$ mb and $\epsilon = 0.055$. The shaded band indicates the region predicted to be excluded for the Odderon signal if we were to use the upper limit for $\sigma(\gamma p \rightarrow f_2 p)$ of 16 nb found at HERA [52], rather than 1 nb

The dashed curves in Fig. 2 show the possible effect of adding the secondary Reggeon amplitude. Again the effect is stronger in the γ -induced case since we expect a larger $\gamma R f_2$ coupling for the fusion with a secondary Reggeon, see (31) and (32).

Figure 2 clearly illustrates the importance of the survival factors with respect to the f_2 additional interactions with the nucleons in the heavy ion, both on the value of the

cross section and its rapidity dependence. Note also that for $\sigma_{\text{tot}}(f_2 N) = 0$ in Fig. 2a, that is when $S_{f_2 N} = 1$ the cross section increases with rapidity, while it decreases if we take the VDM form given by (17) with $\sigma_0 = 15.7$ mb and $\epsilon = 0.055$.

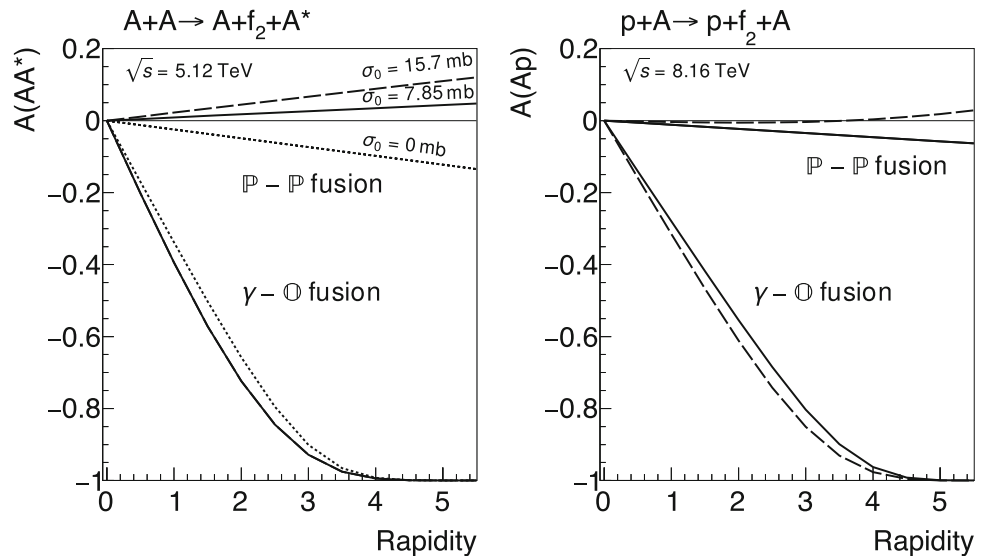
The contributions to the cross section for the process $pA \rightarrow p + f_2 + A$ are plotted in Fig. 3. Here we take $\sigma_0 = 15.7/2$ mb and $\epsilon = 0.055$ in (17), and take the pA collisions to have an energy $\sqrt{s_{NN}} = 8.16$ GeV. For this process we have no enhancement of the γ -induced contributions, that previously was observed in Fig. 2, due to the large transverse surface of the target A^* . Therefore the Odderon contribution is expected to be a few times smaller than that due to Pomeron-Pomeron fusion.

Figure 4 shows that the asymmetry of the Pomeron-induced cross section is small. Without secondary Reggeons it is caused by the non-zero slope, α'_p of the Pomeron trajectory (and gives a small negative asymmetry $A(AA^*) < 0$) while the energy dependence of the absorptive cross section gives a small positive asymmetry ($A(AA^*) > 0$). Recall that without the f_2 absorption the secondary Reggeon contributions do not produce an additional asymmetry. For the photon-induced component we observe in the forward region ($y > 0$) a large negative asymmetry that already by $y = 3$ is close to -1 due to the growth of the photon flux (19) as $x \propto e^{-y}$ decreases.

For pA collisions, the same qualitative behaviour of the asymmetry is observed as in AA collisions, although the asymmetry for the Pomeron-induced process is slightly smaller, and the photon-induced asymmetry approaches -1 at slightly larger rapidities, as seen by comparing the plots in Fig. 4.

Recall, however, the possibility mentioned in Sect. 2.4 that the Pomeron-Pomeron fusion background may be suppressed. The dominant Pomeron-induced background will

Fig. 4 Predictions for the Pomeron–Pomeron and γ -Odderon fusion contributions to the asymmetry as a function of the rapidity of the f_2 meson produced in the process $AA \rightarrow A + f_2 + A^*$ (that is (26) plotted in the left-hand diagram) and in the process $pA \rightarrow p + f_2 + A$ (that is (25) plotted in the right-hand diagram). We also show the effect of changing $\sigma_{\text{tot}}(f_2 N)$ from 0 to forms given by (17) with $\sigma_0 = 15.7/2$ or 15.7 mb and $\epsilon = 0.055$. The effects of including secondary Reggeon-exchange terms only change the predictions within the limits of the σ_0 predictions



then be caused by fusion with a secondary Reggeon. In such a case there will be a large positive asymmetry in Fig. 4 (right) since when the p beam energy is larger than the energy of the nucleon in the ion, the dominant diagram is that where the secondary Reggeon couples to the ion A and thus the f_2 meson goes in the direction of ion.

In summary, assuming an Odderon cross section $\sigma_{\text{Odd}} = 1$ nb in (22), the exclusive f_2 photo-production cross-section in the forward region for $AA \rightarrow A + f_2 + A^*$ processes is expected to be an order-of-magnitude larger than for Pomeron–Pomeron fusion in AA collisions already at $y = 2$ where the secondary Reggeon(s) contribution is still small. Now the major background is caused by the trivial $\gamma\gamma \rightarrow f_2$ process of Sect. 5.1. Thus in the AA case we have a chance to observe the Odderon signal in the $f_2 \rightarrow \pi^0\pi^0$ mode if the corresponding σ_{Odd} cross section exceeds 0.3–0.5 nb.⁸

In pA collisions the expected Odderon signal is a factor of 5 smaller than that due to Pomeron–Pomeron fusion. The asymmetries $A(pA)$ and $A(AA^*)$ are predicted to be similar in all photo-produced processes, and are largely absent in Pomeron–Pomeron fusion.

7 Conclusions

The dependence of the cross section on the rapidity of a centrally produced meson is studied in proton – heavy ion (pA) and in heavy ion-ion (AA) interactions in (semi) exclusive processes (CEP*). We consider the contributions due to production by Pomeron–Pomeron, Pomeron–Reggeon, γ -Odderon, $\gamma\rho$ and $\gamma\omega$ fusion. The presence of a secondary

Reggeon is found to be noticeable in the forward direction of the produced meson, especially when the meson rapidity becomes close to that of the heavy ion. Recall that with LHC kinematics the rapidity of a heavy ion beam is about one unit smaller than that for the proton beam. Thus in the forward direction the rapidity difference between the nucleon N in the ion and the produced meson is not large and the contribution of the secondary Reggeon is not sufficiently suppressed.

We emphasize that the additional interactions of the produced meson with the nucleons in the ion fills the rapidity gap and destroys the exclusivity of the events. This effect is encoded in the gap survival factors. Since the cross section of an additional interaction depends on the meson–nucleon energy, this leads to an additional rapidity dependence of the CEP* cross section. However, all these effects are much weaker than the rapidity dependence of the photon flux emitted by the heavy ion. As an example we present estimates of the cross section for C-even f_2 meson. The CEP of a C-even f_2 meson can arise from the fusion of either two C-odd exchanges or two C-even exchanges. That is respectively γ -Odderon or Pomeron–Pomeron fusion. The difference in the rapidity behaviour of these two contributions to f_2 production helps to extract the Odderon signal.

Of course, the Odderon couplings are not known. However reasonably justified values (by matching with lowest-order QCD calculation [19]) provide estimates which show that, in the process $AA \rightarrow A + f_2 + A^*$, the Odderon-induced signal may exceed by a few times the Pomeron-induced background. On the other hand for pA collisions, $pA \rightarrow p + f_2 + A$, the expected Odderon signal is a few times smaller than that due to the Pomeron–Pomeron background.

A particularly interesting possibility to reveal the difference between the two production mechanisms is to measure the forward–backward asymmetries (25) or (26), correspond-

⁸ Note that the $\gamma\gamma \rightarrow f_2$ contribution can be well controlled. The $f_2 \rightarrow \gamma\gamma$ width is well known while the photon flux for the particular kinematics of the experiment can be monitored via the pure QED $\mu^+\mu^-$ pair production process.

ing to the interchange of the proton and the ion or of the broken (A^*) and unbroken (A) ions. We see from Fig. 4 that for γ -Odderon fusion the asymmetry approaches its maximum value in the forward direction, unlike the behaviour for Pomeron–Pomeron fusion where the asymmetry is less than about 0.1.

Acknowledgements We thank Tara Shears for valuable discussions. RMcN and MGR thank the IPPP at the University of Durham for hospitality.

Data Availability Statement This manuscript has no associated data or the data will not be deposited. [Authors' comment: Typical theoretical predictions are shown. There are no corresponding experimental data.]

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit <http://creativecommons.org/licenses/by/4.0/>. Funded by SCOAP³.

References

- W. Ochs, J. Phys. G **40**, 043001 (2013). [arXiv:1301.5183](#) [hep-ph]
- A. Kirk, Int. J. Mod. Phys. A **29**(28), 1446001 (2014). [arXiv:1408.1196](#) [hep-ex]
- M. Albrow, Int. J. Mod. Phys. A **29**(28), 1446014 (2014)
- M. Albrow, AIP Conf. Proc. **1819**(1), 040008 (2017). [arXiv:1701.09092](#) [hep-ex]
- M.A. Braun, [arXiv:hep-ph/9805394](#)
- C. Ewerz, [arXiv:hep-ph/0306137](#)
- C. Ewerz, [arXiv:hep-ph/0511196](#)
- J. Kwiecinski, M. Praszalowicz, Phys. Lett. B **94**, 413 (1980)
- J. Bartels, Nucl. Phys. B **175**, 365 (1980)
- V.V. Barakhovsky, I.R. Zhitnitsky, A.N. Shelkovenko, Phys. Lett. B **267**, 532 (1991)
- M.G. Ryskin, Eur. Phys. J. C **2**, 339 (1998)
- E.R. Berger, A. Donnachie, H.G. Dosch, O. Nachtmann, Eur. Phys. J. C **14**, 673 (2000)
- I.P. Ivanov, N.N. Nikolaev, I.F. Ginzburg, Sci. Cult. Ser. -Phys. **21**, 728 (2002). [arXiv:hep-ph/0110181](#)
- I.F. Ginzburg, I.P. Ivanov, N.N. Nikolaev, Eur. Phys. J. Direct **5**(1), 002 (2003). [arXiv:hep-ph/0207345](#)
- P. Hagler, B. Pire, L. Szymanowski, O.V. Teryaev, Phys. Lett. B **535**, 117 (2002). Erratum: [Phys. Lett. B **540** (2002) 324] [[arXiv:hep-ph/0202231](#)]
- M.V.T. Machado, Phys. Rev. D **86**, 014029 (2012). [arXiv:1112.0271](#) [hep-ph]
- A. Bolz, C. Ewerz, M. Maniatis, O. Nachtmann, M. Sauter, A. Schoning, JHEP **1501**, 151 (2015). [arXiv:1409.8483](#) [hep-ph]
- V.P. Goncalves, Eur. Phys. J. C **79**(5), 408 (2019). [arXiv:1811.07622](#) [hep-ph]
- L.A. Harland-Lang, V.A. Khoze, A.D. Martin, M.G. Ryskin, Phys. Rev. D **99**(3), 034011 (2019). [arXiv:1811.12705](#) [hep-ph]
- A. Donnachie, P.V. Landshoff, Nucl. Phys. B **231**, 189 (1984)
- A. Donnachie, P.V. Landshoff, Phys. Lett. B **296**, 227 (1992)
- D. Barberis et al., [WA102 Collaboration]. Phys. Lett. B **462**, 462 (1999). [arXiv:hep-ex/9907055](#)
- L.A. Harland-Lang, V.A. Khoze, M.G. Ryskin, Eur. Phys. J. C **79**, 39 (2019). [arXiv:1810.06567](#)
- L. Frankfurt, V. Guzey, M. Strikman, M. Zhalov, Phys. Lett. B **752**, 51 (2016). [arXiv:1506.07150](#)
- C. Ciofi degli Atti, B.Z. Kopeliovich, C.B. Mezzetti, I.K. Potashnikova, I. Schmidt, Phys. Rev. C **84**, 025205 (2011). [arXiv:1105.1080](#)
- R.D. Woods, D.S. Saxon, Phys. Rev. **95**, 577 (1954)
- C.M. Tarbert et al., Phys. Rev. Lett. **112**, 242582 (2014)
- A.B. Jones, B.A. Brown, Phys. Rev. C **98**, 067384 (2014)
- J.A. Crittenden, Exclusive production of neutral vector mesons at the electron–proton collider HERA. Springer, Berlin, 100 (1997). [arXiv:hep-ex/9704009](#)
- J.J. Sakurai, Ann. Phys. **11**, 1 (1960)
- T.H. Bauer, R.D. Spital, D.R. Yennie, F.M. Pipkin, Rev. Mod. Phys. **50**, 261 (1978). Erratum: [Rev. Mod. Phys. **51**, 407 (1979)]
- G. Bertsch et al., Phys. Rev. Lett. **47**, 297 (1981)
- B.Z. Kopeliovich, L.I. Lapidus, A.B. Zaslavchikov, JETP Lett. **33**, 595 (1981)
- V.A. Khoze, A.D. Martin, M.G. Ryskin, Eur. Phys. J. C **23**, 311 (2002). [arXiv:hep-ph/0111078](#)
- A.B. Kaidalov, V.A. Khoze, A.D. Martin, M.G. Ryskin, Eur. Phys. J. C **31**, 387 (2003). [arXiv:hep-ph/0307064](#)
- L.A. Harland-Lang, V.A. Khoze, M.G. Ryskin, W.J. Stirling, Int. J. Mod. Phys. A **29**, 1430031 (2014). [arXiv:1405.0018](#) [hep-ph]
- V.A. Khoze, A.D. Martin, M.G. Ryskin, Eur. Phys. J. C **19**, 477 (2001). Erratum: [Eur. Phys. J. C **20**, 599 (2001)] [[arXiv:hep-ph/0011393](#)]
- L. Bergstrom, G. Hulth, H. Snellman, Z. Phys. C **16**, 263 (1983)
- Z.P. Li, F.E. Close, T. Barnes, Phys. Rev. D **43**, 2161 (1991)
- S. Uehara et al., [Belle Collaboration]. Phys. Rev. D **78**, 052004 (2008). [arXiv:0805.3387](#) [hep-ex]
- A. Breakstone et al., [Ames-Bologna-CERN-Dortmund-Heidelberg-Warsaw Collaboration]. Z. Phys. C **31**, 185 (1986)
- A. Breakstone et al., [ABCDHW Collaboration]. Z. Phys. C **40**, 41 (1988)
- T. Akesson et al., [Axial Field Spectrometer Collaboration]. Phys. Lett. B **133**, 268 (1983)
- T. Akesson et al., [Axial Field Spectrometer Collaboration], Nucl. Phys. B **264**, 154 (1986)
- G. Gutierrez, M.A. Reyes, Int. J. Mod. Phys. A **29**(28), 1446008 (2014). [arXiv:1409.8243](#) [hep-ex]
- M. Albrow, invited talk at the the Low-x workshop, Nicosia, Cyprus, 26–31 August (2019)
- R. McNulty [LHCb collaboration], [arXiv:1711.06668](#)
- G. Baur, L.G. Ferreira Filho, Nucl. Phys. A **518**, 786 (1990)
- K. Hencken, D. Trautmann, G. Baur, Z. Phys. C **68**, 473 (1995). [arXiv:nucl-th/9503004](#)
- J. Bartels, L.N. Lipatov, G.P. Vacca, Phys. Lett. B **477**, 178 (2000)
- P. Newman, M. Wing, Rev. Mod. Phys. **86**, 1037 (2014). [arXiv:1308.3368](#)
- T. Berndt, [H1 collaboration], Acta Phys. Polon. B **33**, 3499 (2002)
- A. M. Sirunyan et al., Study of central exclusive $\pi^+\pi^-$ production in proton–proton collisions at $\sqrt{s} = 5.02$ and 13 TeV. [CMS Collaboration] (2020). [arXiv:2003.02811](#) [hep-ex]